

# CS502

## Fundamentals of Algorithms

### Important subjective

#### Lec 1 - Introduction

1. **What is the purpose of an introduction in academic writing?**

Answer: The purpose of an introduction in academic writing is to provide context and background information for the reader, establish the author's credibility, and present the thesis statement.

**Why is it important to capture the reader's attention in the introduction?**

Answer: It is important to capture the reader's attention in the introduction because it motivates them to continue reading or listening to the work and sets the tone for the entire piece.

**What are some techniques that can be used to capture the reader's attention in the introduction?**

Answer: Some techniques that can be used to capture the reader's attention in the introduction include using a provocative question or statement, providing surprising facts or statistics, or using vivid imagery.

**What is a thesis statement and where is it typically located in the introduction?**

Answer: A thesis statement is a sentence or two that summarizes the main point or argument of the work. It is typically located at the end of the introduction.

**What should be included in the background information presented in the introduction?**

Answer: The background information presented in the introduction should be relevant to the topic and provide context for the reader. It can include historical, social, or cultural information that is important for understanding the work.

**How can the introduction be used to establish the author's credibility?**

Answer: The introduction can be used to establish the author's credibility by presenting relevant credentials, demonstrating knowledge of the topic, or citing reputable sources.

**What is the purpose of providing an overview of the main points in the introduction?**

Answer: The purpose of providing an overview of the main points in the introduction is to give the reader a roadmap for the work and help them understand the organization of the piece.

**How should the tone of the introduction be set?**

Answer: The tone of the introduction should be set by considering the audience, the purpose of the work, and the author's personal style. It should be professional and appropriate for the context.

**Can the introduction be revised after the rest of the work is written?**

Answer: Yes, the introduction can be revised after the rest of the work is written to ensure that it

accurately reflects the content and organization of the piece.

**What are some common mistakes to avoid in the introduction?**

Answer: Common mistakes to avoid in the introduction include providing irrelevant information, making unsupported claims, using an inappropriate tone, or failing to clearly present the thesis statement.

## Lec 2 - Asymptotic Notation

1. **What is the purpose of using asymptotic notation in algorithm analysis?**

Answer: The purpose of using asymptotic notation is to describe the growth rate of a function and simplify the analysis of algorithms by ignoring constant factors and lower order terms.

**What does Big O notation represent?**

Answer: Big O notation represents the upper bound of a function or the worst-case running time of an algorithm.

**What does Omega notation represent?**

Answer: Omega notation represents the lower bound of a function or the best-case running time of an algorithm.

**What does Theta notation represent?**

Answer: Theta notation represents both the upper and lower bounds of a function or the tightest possible bounds on the running time of an algorithm.

**What is the difference between worst-case and average-case running time?**

Answer: Worst-case running time represents the maximum time required for an algorithm to complete, while average-case running time represents the expected time required for an algorithm to complete.

**Which notation is used to describe the growth rate of an algorithm that has constant running time?**

Answer: Theta notation is used to describe the growth rate of an algorithm that has constant running time.

**Which notation is used to describe the best-case running time of an algorithm?**

Answer: Omega notation is used to describe the best-case running time of an algorithm.

**Which notation is used to describe the tightest possible bounds on the running time of an algorithm?**

Answer: Theta notation is used to describe the tightest possible bounds on the running time of an algorithm.

**What is the relationship between  $f(n)$  and  $g(n)$  if  $f(n)$  is  $O(g(n))$ ?**

Answer: If  $f(n)$  is  $O(g(n))$ , it means that  $f(n)$  grows no faster than  $g(n)$  as  $n$  approaches infinity.

**What is the relationship between  $f(n)$  and  $g(n)$  if  $f(n)$  is  $\Omega(g(n))$ ?**

Answer: If  $f(n)$  is  $\Omega(g(n))$ , it means that  $f(n)$  grows at least as fast as  $g(n)$  as  $n$  approaches infinity.

## Lec 3 - Divide and Conquer Strategy

### 1. What is the Divide and Conquer strategy?

Answer: The Divide and Conquer strategy is a problem-solving approach that involves breaking down a complex problem into smaller subproblems, solving them recursively, and combining the solutions to obtain the final solution.

### What is the time complexity of the Divide and Conquer strategy?

Answer: The time complexity of the Divide and Conquer strategy is usually  $O(n \log n)$ , where  $n$  is the size of the problem.

### What is the difference between top-down and bottom-up approaches in the Divide and Conquer strategy?

Answer: In the top-down approach, the problem is broken down into smaller subproblems until the subproblems become simple enough to solve directly. In the bottom-up approach, the simple subproblems are solved first and then combined to solve the larger problem.

### What is the main advantage of the Divide and Conquer strategy?

Answer: The main advantage of the Divide and Conquer strategy is that it reduces the time complexity of solving complex problems.

### Give an example of a problem that can be solved using the Divide and Conquer strategy.

Answer: Merge sort is an example of a problem that can be solved using the Divide and Conquer strategy.

### What is the role of recursion in the Divide and Conquer strategy?

Answer: Recursion is used to solve the smaller subproblems in the Divide and Conquer strategy.

### What is the base case in the Divide and Conquer strategy?

Answer: The base case is the simplest form of the subproblem that can be solved directly without further division.

### How does the Divide and Conquer strategy relate to dynamic programming?

Answer: The Divide and Conquer strategy is a recursive approach that breaks down a problem into smaller subproblems. Dynamic programming, on the other hand, is an optimization technique that solves subproblems once and stores the solutions for later use.

### Can the Divide and Conquer strategy be used to solve non-numerical problems?

Answer: Yes, the Divide and Conquer strategy can be used to solve non-numerical problems as long as they can be broken down into smaller subproblems.

### What is the main disadvantage of the Divide and Conquer strategy?

Answer: The main disadvantage of the Divide and Conquer strategy is that it may require additional memory to store the solutions of the subproblems.

## Lec 4 - Sorting

### 1. What is sorting?

Answer: Sorting is the process of arranging items in a specific order, typically numerical or alphabetical order, to make them easier to access, search, and analyze.

### What is the difference between stable and unstable sorting algorithms?

Answer: Stable sorting algorithms maintain the relative order of equal elements in the sorted output, while unstable sorting algorithms do not guarantee this.

### What is the worst-case time complexity of bubble sort?

Answer: The worst-case time complexity of bubble sort is  $O(n^2)$ , where  $n$  is the number of items being sorted.

### What is quick sort, and how does it work?

Answer: Quick sort is a divide-and-conquer sorting algorithm that works by partitioning an array into two sub-arrays, one containing elements less than a pivot element, and the other containing elements greater than the pivot. It then recursively sorts the sub-arrays.

### What is the difference between in-place and out-of-place sorting algorithms?

Answer: In-place sorting algorithms sort the input array by modifying it, while out-of-place sorting algorithms sort the input array by creating a new, sorted array.

### What is insertion sort, and how does it work?

Answer: Insertion sort is a simple sorting algorithm that works by iterating through an array, comparing each element with the preceding elements, and swapping them if they are out of order.

### What is the difference between comparison-based and non-comparison-based sorting algorithms?

Answer: Comparison-based sorting algorithms compare elements in the input array to determine their order, while non-comparison-based sorting algorithms use other methods, such as counting or hashing, to sort the elements.

### What is merge sort, and how does it work?

Answer: Merge sort is a divide-and-conquer sorting algorithm that works by dividing an array into two halves, recursively sorting each half, and then merging the two sorted halves into a single sorted array.

### What is radix sort, and how does it work?

Answer: Radix sort is a non-comparison-based sorting algorithm that works by sorting elements based on their digits or characters, from the least significant to the most significant.

### What is the best-case time complexity of quick sort?

Answer: The best-case time complexity of quick sort is  $O(n \log n)$ , where  $n$  is the number of items being sorted.

## Lec 5 - Linear Time Sorting

### 1. What is linear time sorting?

Answer: Linear time sorting is a class of sorting algorithms that can sort a given set of data in linear time, meaning the time complexity is proportional to the number of elements being sorted.

### What is the time complexity of counting sort?

Answer: The time complexity of counting sort is  $O(n)$ , where  $n$  is the number of elements being sorted.

### What is the difference between comparison-based sorting algorithms and linear time sorting algorithms?

Answer: Comparison-based sorting algorithms compare elements to determine their order, while linear time sorting algorithms use other methods to determine their order, such as counting or bucketing.

### Can counting sort be used to sort negative integers?

Answer: No, counting sort cannot be used to sort negative integers because it requires non-negative integers as input.

### What is the purpose of the bucket sort algorithm?

Answer: The bucket sort algorithm divides the input data into a number of smaller buckets, which are then sorted using another algorithm. The sorted buckets are then concatenated to form the final sorted output.

### What is the time complexity of radix sort?

Answer: The time complexity of radix sort is  $O(d(n+k))$ , where  $d$  is the number of digits in the maximum element,  $n$  is the number of elements being sorted, and  $k$  is the maximum value of a digit.

### Is radix sort a stable sorting algorithm?

Answer: Yes, radix sort is a stable sorting algorithm because it maintains the relative order of equal elements.

### How does counting sort work?

Answer: Counting sort works by counting the number of occurrences of each element in the input, and then using this information to determine the final sorted order.

### What is the difference between bucket sort and radix sort?

Answer: Bucket sort divides the input into a fixed number of equally sized buckets, while radix sort divides the input into a variable number of buckets based on the value of a digit.

### Can linear time sorting algorithms be used for all types of data?

Answer: No, linear time sorting algorithms have certain restrictions on the types of data they can sort, such as requiring non-negative integers for counting sort.

## Lec 6 - Dynamic Programming

### 1. What is Dynamic Programming?

Answer: Dynamic Programming is a problem-solving technique used to solve complex optimization problems by breaking them down into smaller, simpler subproblems and solving them recursively.

### What are the two approaches to Dynamic Programming?

Answer: The two approaches to Dynamic Programming are top-down (memoization) and bottom-up (tabulation).

### What is memoization in Dynamic Programming?

Answer: Memoization is an approach in Dynamic Programming where solutions to subproblems are stored in a table, which can be accessed later to solve larger subproblems.

### What is tabulation in Dynamic Programming?

Answer: Tabulation is an approach in Dynamic Programming where solutions to subproblems are computed iteratively and stored in a table, which can be used to solve larger subproblems.

### What is the difference between memoization and tabulation in Dynamic Programming?

Answer: Memoization involves solving subproblems recursively and storing the solutions in a table, while tabulation involves computing the solutions iteratively and storing them in a table.

### What are the advantages of using Dynamic Programming?

Answer: The advantages of using Dynamic Programming include improved efficiency, reduced computational resources, and the ability to solve complex optimization problems.

### What is the principle of optimality in Dynamic Programming?

Answer: The principle of optimality in Dynamic Programming states that an optimal solution to a problem can be obtained by combining optimal solutions to its subproblems.

### What is the time complexity of Dynamic Programming?

Answer: The time complexity of Dynamic Programming depends on the problem being solved and the approach used.

### What are the common applications of Dynamic Programming?

Answer: The common applications of Dynamic Programming include robotics, operations research, computer science, economics, and finance.

### What are the limitations of using Dynamic Programming?

Answer: The limitations of using Dynamic Programming include high memory requirements, difficulty in solving some problems, and the need for mathematical knowledge.

## Lec 7 - Greedy Algorithms

### 1. What is a greedy algorithm, and what is its basic approach?

Answer: A greedy algorithm is an algorithmic paradigm that follows the problem-solving heuristic of making the locally optimal choice at each stage with the hope of finding a global optimum. The basic approach of a greedy algorithm is to make the best possible choice at each step without considering the overall effect on the solution.

### What is the difference between a greedy algorithm and a dynamic programming algorithm?

Answer: In a greedy algorithm, we make the locally optimal choice at each stage without considering the overall effect on the solution. In contrast, dynamic programming is a bottom-up approach that breaks the problem into smaller subproblems, solves each subproblem once, and saves the result for future use.

### What is the fractional knapsack problem, and how can it be solved using a greedy algorithm?

Answer: The fractional knapsack problem is a variation of the classic knapsack problem, where the items can be divided into smaller pieces. A greedy algorithm can be used to solve the fractional knapsack problem by sorting the items by their value-to-weight ratio and adding them to the knapsack until it is full.

### Can a greedy algorithm be used to solve the minimum spanning tree problem? If so, how?

Answer: Yes, a greedy algorithm can be used to solve the minimum spanning tree problem. The most commonly used algorithm for this is Prim's algorithm, which starts with an arbitrary vertex and repeatedly adds the edge with the smallest weight that connects a vertex in the tree to one outside the tree.

### What is the Huffman coding algorithm, and how does it work?

Answer: Huffman coding is a lossless data compression algorithm that uses variable-length codes to represent data. The algorithm works by building a Huffman tree based on the frequency of occurrence of each symbol in the input. The tree is then used to generate the variable-length codes for each symbol.

### What is the job sequencing problem, and how can it be solved using a greedy algorithm?

Answer: The job sequencing problem is a scheduling problem where a set of jobs with different deadlines and profits needs to be scheduled on a single machine. A greedy algorithm can be used to solve the job sequencing problem by sorting the jobs by their profits in descending order and scheduling them in the order of their sorted list.

### What is the coin change problem, and how can it be solved using a greedy algorithm?

Answer: The coin change problem is a classic problem where a given sum of money needs to be paid using the minimum number of coins. A greedy algorithm can be used to solve the coin change problem by repeatedly selecting the largest coin denomination that is less than or equal to the remaining amount.

### Can a greedy algorithm be used to solve the traveling salesman problem? If not, why not?

Answer: No, a greedy algorithm cannot be used to solve the traveling salesman problem



because it does not have the optimal substructure property required for a greedy algorithm to work.

**What is the knapsack problem, and how can it be solved using a greedy algorithm?**

Answer: The knapsack problem is a classic optimization problem where a set of items with different weights and values needs to be packed into a knapsack with a limited capacity. A greedy algorithm can be used to solve the knapsack problem by sorting the items by their value-to-weight ratio and adding them to the knapsack until it is full.

**What is the difference between a greedy algorithm and a backtracking algorithm?**

Answer: In a greedy algorithm, we make the locally optimal choice at each stage without considering the overall effect on the solution. In contrast, backtracking is a recursive approach that explores all possible solutions to a problem and backtracks when a dead end is reached.

## Lec 8 - Graphs

### 1. What is a vertex in a graph?

A vertex, also known as a node, is a fundamental unit of a graph that represents an entity or object.

### What is an edge in a graph?

An edge, also known as an arc, is a connection between two vertices that represents a relationship between them.

### What is a directed graph?

A directed graph is a graph where the edges have a direction or orientation.

### What is an undirected graph?

An undirected graph is a graph where the edges have no direction or orientation.

### What is a weighted graph?

A weighted graph is a graph where the edges have a numerical value assigned to them.

### What is a connected graph?

A connected graph is a graph where there is a path between any two vertices in the graph.

### What is a cycle in a graph?

A cycle is a sequence of vertices and edges that starts and ends at the same vertex.

### What is a tree?

A tree is a connected acyclic graph, which means that there are no cycles in the graph.

### What is a bipartite graph?

A bipartite graph is a graph where the vertices can be divided into two sets, such that each edge connects a vertex from one set to a vertex in the other set.

### What is a path in a graph?

A path is a sequence of vertices and edges that connects two vertices in a graph.

## Lec 9 - Complexity Theory

### 1. What is the difference between time complexity and space complexity?

Answer: Time complexity measures the amount of time taken by an algorithm to solve a problem, whereas space complexity measures the amount of memory used by an algorithm to solve a problem.

### What is the significance of the class P in complexity theory?

Answer: The class P contains all decision problems that can be solved in polynomial time. This class is important because many important problems in computer science, such as sorting and searching, are known to belong to P.

### What is the meaning of the term "hardness" in complexity theory?

Answer: The term "hardness" is used to describe the difficulty of a problem. A problem is said to be hard if it is unlikely to have an efficient algorithmic solution.

### What is the difference between the classes NP and NP-complete?

Answer: The class NP contains all decision problems that can be verified in polynomial time. The class NP-complete contains all problems that are at least as hard as the hardest problems in NP.

### What is the significance of the class NP-hard in complexity theory?

Answer: The class NP-hard contains all problems that are at least as hard as the hardest problems in NP. These problems are important because they are believed to be very difficult, and many of them are used as benchmarks for the performance of algorithms.

### What is the significance of the class PSPACE in complexity theory?

Answer: The class PSPACE contains all decision problems that can be solved using polynomial space. This class is important because it contains many important problems, such as the problem of determining whether a chess position is a win, loss, or draw.

### What is the significance of the class EXP in complexity theory?

Answer: The class EXP contains all decision problems that can be solved using exponential time. This class is important because it contains many problems that are believed to be very difficult, such as the problem of factoring large integers.

### What is the meaning of the term "reduction" in complexity theory?

Answer: The term "reduction" refers to the process of transforming one problem into another problem. Reductions are used to show that one problem is at least as hard as another problem.

### What is the difference between a decision problem and an optimization problem?

Answer: A decision problem asks whether a certain condition holds, whereas an optimization problem asks for the best solution to a certain condition. In other words, a decision problem is a yes-or-no question, whereas an optimization problem is a question of finding the best answer.

### What is the significance of the traveling salesman problem in complexity theory?

Answer: The traveling salesman problem is a well-known problem in complexity theory that asks for the shortest possible route that visits each of a given set of cities and returns to the starting city. It is significant because it is an example of an NP-complete problem, which is believed to be very difficult.

